

① $P = dgh$

a) $P = 1000 \cdot 9,8 \cdot 3 = \underline{29400 \text{ Pa}}$

b) $P = 1030 \cdot 9,8 \cdot 3 = \underline{30282 \text{ Pa}}$

② $P = dgh \rightarrow h = \frac{P}{dg} = \frac{50650}{1030 \cdot 9,8} = \underline{5,02 \text{ m}}$

③ $\frac{F_1}{S_1} = \frac{F_2}{S_2} \Rightarrow F_1 S_2 = F_2 S_1 \Rightarrow \boxed{S_2 = \frac{F_2 S_1}{F_1}}$

$F_2 = 1000 \text{ kg} \cdot 9,8 \text{ m/s}^2 = 9800 \text{ N}$

$S_2 = \frac{9800 \text{ N} \cdot 20 \text{ cm}^2}{490 \text{ N}} = \underline{400 \text{ cm}^2}$

④ Primero hay que calcular la presión del agua sobre el tapón: $h = 10 \text{ cm} = 0,1 \text{ m}$

$P = dgh = 1000 \cdot 9,8 \cdot 0,1 = 980 \text{ Pa}$

Ahora podemos calcular la fuerza que el agua ejerce sobre el tapón:

$P = \frac{F}{S} \Rightarrow F = P \cdot S$

$S = \pi R^2$

$R = 3 \text{ cm} = 0,03 \text{ m}$

$$S = \pi \cdot (0,03 \text{ m})^2 = 0,0028 \text{ m}^2$$

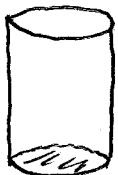
$$F = p S = 980 \cdot 0,0028 = \boxed{2,7 \text{ N}}$$

$$\textcircled{5} \quad \boxed{S_2 = 6 S_1} \quad F_1 = 240 \text{ N}$$

$$\frac{F_1}{S_1} = \frac{F_2}{S_2} \Rightarrow F_1 S_2 = F_2 S_1 \Rightarrow F_2 = \frac{F_1 S_2}{S_1} \Rightarrow$$

$$F_2 = \frac{F_1 \cancel{6 S_1}}{\cancel{S_1}} = 6 F_1 = 6 \cdot 240 = \boxed{1440 \text{ N}}$$

$\textcircled{6}$



$$R = 5 \text{ m} \quad F = 6923700 \text{ N}$$

$$S = \pi R^2$$

$$S = \pi \cdot 5^2 = 78,5 \text{ m}^2$$

$$p = \frac{F}{S} = \frac{6923700}{78,5} = 88200 \text{ Pa}$$

$$p = d g h \Rightarrow h = \frac{p}{d g} = \frac{88200}{1000 \cdot 9,8} = \boxed{9 \text{ m}}$$

$$\textcircled{7} \quad p = d g h \Rightarrow d = \frac{p}{g h} = \frac{131690}{9,8 \cdot 5} = 2688 \frac{\text{kg}}{\text{m}^3}$$

$$d = 2688 \frac{\text{kg}}{\text{m}^3} \cdot \frac{1000 \text{ g}}{1 \text{ kg}} \cdot \frac{1 \text{ m}^3}{1000000 \text{ cm}^3} = \boxed{2,69 \text{ g/cm}^3}$$

8)

$$\left. \begin{aligned} P_{\text{Hg}} &= d_{\text{Hg}} \cdot g \cdot h_{\text{Hg}} \\ P_{\text{agua}} &= d_{\text{agua}} \cdot g \cdot h_{\text{agua}} \end{aligned} \right\} P_{\text{Hg}} = P_{\text{agua}}$$

$$d_{\text{agua}} \cdot g \cdot h_{\text{agua}} = d_{\text{Hg}} \cdot g \cdot h_{\text{Hg}}$$

$$1000 \cdot h_{\text{agua}} = 13600 \cdot 1$$

$$h_{\text{agua}} = \frac{13600}{1000} = \underline{13,6 \text{ m}}$$

9)

$$F_2 = 15 F_1$$

$$\frac{F_1}{S_1} = \frac{F_2}{S_2} \Rightarrow F_1 S_2 = F_2 S_1 \Rightarrow$$

$$\Rightarrow \frac{S_2}{S_1} = \frac{F_2}{F_1} = \frac{15 F_1}{F_1} = 15$$

$$\boxed{S_2 = 15 S_1}$$

El pistón mayor debe tener una superficie 15 veces mayor que la del pistón más pequeño.